Pre-SUSY 2021: The Summer School on Supersymmetry and Unification of Fundamental Interactions



## Hints of new physics in semi-leptonic B decays

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## Background

- □ Theoretical framework
- Results and discussions
  - > Flavor-changing-neutral-current(FCNC)  $b \rightarrow s l l$  decays
  - > Charged-current(CC)  $b \rightarrow c \tau \nu$  decays
- □ Summary and outlook



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## Frontiers in high energy physics

US Particle Physics Scientific Opportunities: A Strategic Plan for the Next 10 Years



CMS&ATLAS: higgs; supersymmetric Particles; new interactions; ...

LCHb&Bellell&BESIII: new hadronic States; heavy flavor physics (B physics); ...

Indirect detection of NP via the test of the lepton universality (LU) is one of the hot topics.

## □ SM Lagrangian

$$\begin{split} \mathcal{L}_{SM} &= -\frac{1}{4} G^{a}_{\mu\nu} G^{a\mu\nu} - \frac{1}{4} W^{i}_{\mu\nu} W^{i\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + \frac{\theta}{16\pi^2} G^{a}_{\mu\nu} \tilde{G}^{a\mu\nu} \\ &+ \sum_{\psi = \{l, e, u, d, q\}} \bar{\psi} i \vec{D} \psi - \left[ \bar{l} H Y_l e + \bar{q} H Y_d d + \bar{q} \tilde{H} Y_u u + \text{hc.} \right] \\ &+ D_{\mu} H^{\dagger} D^{\mu} H + \frac{m_h^2}{2} (H^{\dagger} H) - \lambda (H^{\dagger} H)^2 \\ D_{\mu} \sim \partial_{\mu} + ig_s G^{a}_{\mu} T^a + ig W^{i}_{\mu} t^i + ig' B_{\mu} \end{split}$$

#### **Standard Model of Elementary Particles**



## Lepton universality (LU) in the Standard Model (SM)



From the 2020 PDG averages

$$\frac{B(W^+ \to \mu^+ \nu)}{B(W^+ \to e^+ \nu)} = 0.991 \pm 0.018$$
  

$$\frac{B(W^+ \to \tau^+ \nu)}{B(W^+ \to e^+ \nu)} = 1.043 \pm 0.024$$
  

$$\frac{B(W^+ \to \tau^+ \nu)}{B(W^+ \to \mu^+ \nu)} = 1.070 \pm 0.026$$
  

$$\frac{B(Z \to \mu^+ \mu^-)}{B(Z \to e^+ e^-)} = 1.0009 \pm 0.0032$$

Predictions in the SM: ~1; the largest deviation about 2.7 sigma

## Lepton universality (LU) in the Standard Model (SM)

ATLAS: 139 fb pp collision data at 13 TeV

Nature Physics 17 (2021)813





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## However, some LU violation signals ( $R_D$ , $R_{D^*}$ , $R_K$ , $R_{K^*}$ , etc.) in B semi-leptonic decays have shown persistent deviation from the SM

## **Progress in experimental measurements**



## Testing LUV ( $\mu \neq e$ ) in FCNC $b \rightarrow s l l$ decays, i.e., $R_{\kappa}$ and $R_{\kappa^*}$

$$\mathbf{R}^{\mathrm{SM}}_{\mathbf{K}^{(*)}} = \frac{\Gamma(\mathbf{B} \rightarrow \mathbf{K}^{(*)} \mu^+ \mu^-)}{\Gamma(\mathbf{B} \rightarrow \mathbf{K}^{(*)} \mathbf{e}^+ \mathbf{e}^-)} \cong \mathbf{1}$$

 Belle:
 PRL103(2009)171801
 LHCb

 BaBar:
 PRD86(2012)032012
 LHCb

 LHCb:
 PRL113(2014)151601
 Belle:

 LHCb:
 arXiv:
 2103.11769

LHCb: JHEP08(2017)055 LHCb: PRL122(2019)191801 Belle: PRL126 (2019)161801





BELLE



□ Belle 2009 and BaBar 2012 measurements , no anomalies.

□ LHCb 2014 - 2021, the significance of tension with the SM increases 2.6 $\sigma$  - 3.1 $\sigma$  for R<sub>K</sub>. □ For R<sub>K</sub>, the LHCb 2017 measurements deviate from the SM with a significance of ~2.3 $\sigma$ , 2.4 $\sigma$ .

## Testing LUV ( $\tau \neq \mu/e$ ) in $b \rightarrow c \tau \nu$ decays, i.e., $R_D$ and $R_{D^*}$

$$\mathbf{R}_{\mathbf{D}^{(*)}}^{\mathrm{SM}} = \frac{\Gamma(\mathbf{B} \to \mathbf{D}^{(*)} \tau \bar{\nu})}{\Gamma(\mathbf{B} \to \mathbf{D}^{(*)} \ell \bar{\nu})}, \qquad (\ell = \mu, \mathbf{e})$$



- **D** Belle 2019 measurement of  $R_D$  and  $R_{D^*}$  with a semi-leptonic tagging method;
- **D** Belle 2019 measurements are compatible with the SM within  $1.2\sigma$ ;
- □ HFLAV 2019 results are closer to the SM predictions.

## Theoretical approaches to study anomalies in B physics

#### **G** "Top-down" approaches:

• Leptoquark model

Oleg Popov et al, PRD100.035028 Claudia Cornella et al, JHEP07(2019)168 Leandro Da Rold et al, JHEP12(2019)112

• Z' boson model

Ashutosh Kumar Alok et el, EPJC80 (2020)7,682 Wolfgang Altmannshofer et al, PRD101.015004 Siddharth Dwivedi et al, EPJC80 (2020) 3, 263

Two-Higgs-doublet model
 Astrid Ordell et al, PRD100.115038
 Ya-Dong Yang et al, JHEP09(2018)149
 Luigi Delle Rose et al, PRD101.115009

#### **G** "Bottom-up" approach:

• low-energy effective Hamiltonian approach.





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## Low-energy effective Hamiltonian approach





## **DFCNC:** $b \rightarrow s l l$ transition

The low energy effective Hamiltonian at  $O(m_b)$  scale:



- $\blacktriangleright$  Wilson coefficients Ci( $\mu$ ) calculated in perturbation theory at  $\mu = m_w$  and rescaled to  $\mu = m_b$ .
- For a specific decay mode, another important work is to calculate hadronic matrix elements produced by operators involving non-perturbative effects.

## **DFCNC:** $b \rightarrow s l l$ transition

$$G_F V_{tb} V_{ts}^* \frac{\alpha}{4\pi} C_{9(10)} \bar{s}_L \gamma^\mu b_L \bar{\ell} \gamma_\mu (\gamma_5) \ell$$



### **New chirally-flipped operators:**

$$\mathcal{O}_{9(10)}' = \frac{4G_F}{\sqrt{2}} \frac{\alpha}{4\pi} \,\bar{s} \gamma^{\mu} P_R b \,\bar{\ell} \gamma_{\mu}(\gamma_5) \ell$$

 $\blacktriangleright \quad \text{Different values of Wilson coefficients} \quad \mathbf{C}_i^{\mathrm{expt.}} = \mathbf{C}_i^{\mathrm{SM}} + \delta \mathbf{C}_i + \mathbf{C}_i'$ 

> Note that  $O_s$ ,  $O_p$  and  $O_T$  cannot explain  $R_K$  and  $R_{K*}$  from J. Martin Camalich et al, PRL113.241802.

Using the low energy effective Hamiltonian to calculate amplitude and observables

Fitting to experimental data and constraining δCi

## Using the frequentist statistic approach to analyze fit results

#### **Key questions**





## Assuming that the NP only appears in the muon channels and all Wilson coefficients are real.



**\Box** Only the operators  $O_9$ ,  $O_{10}$  instead of  $O_9$ ',  $O_{10}$ ' are favored by the data.



## Interesting decay channels of $b \rightarrow s l l$ decays



**D** Note that  $BR(B \rightarrow K^* \gamma)$  can fix better soft form factors.

E.g: Form factors  $F(q^2)$ : HQEFT

 $F(q^2) = F^{\infty}(q^2) + a_F + b_F q^2 / m_B^2 + \mathcal{O}([q^2 / m_B^2]^2)$ 

Soft form factors



Very clean ( *f<sub>Bs</sub>* has been calculated accurately by the LQCD) FLAG 2019, *EPJC*80(2020)2,113
 Very rare (GIM and helicity suppression)

 $B \rightarrow K \mu^+ \mu^-$  decay



- □ Kinematics range for the 3-body decay is  $q^2 \in [4m_l^2, (m_B m_K)^2]$
- □ There are very complicated non-perturbative effects
- **Charmonium region** cannot be calculated by perturbation theory

## $B \rightarrow K^* (\rightarrow K\pi) \mu^+ \mu^-$ decay

Kinematics of 4-body decay:



**\Box** Focusing on low bins (q<sup>2</sup>≤6 GeV<sup>2</sup>):

► Form factors 
$$F(q^2)$$
: HQEFT  
Power corrections  
 $F(q^2) = F^{\infty}(q^2) + a_F + b_F q^2 / m_B^2 + O([q^2 / m_B^2]^2)$ .  
Soft form factors  
► Charm loops  $h_{\lambda}(q^2)$ : HQEFT  
 $h_{\lambda}(q^2) = h_{\lambda}^{\infty}(q^2) + r_{\lambda}(q^2) - r_{\lambda}(q^2) = A_{\lambda} + B_{\lambda} \frac{q^2}{4m_c^2}$ 

$$\frac{d^{(4)}\Gamma}{dq^2d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} I^{(\ell)}(q^2,\theta_\ell,\theta_K,\phi),$$
  

$$\theta_K,\phi) = \left(I_1^s \sin^2\theta_K + I_1^c \cos^2\theta_K + (I_2^s \sin^2\theta_K + I_2^c \cos^2\theta_K) \cos 2\theta_\ell + I_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + (I_6^s \sin^2\theta_K + I_6^c \cos^2\theta_K) \cos \theta_\ell + I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + I_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi\right),$$

$$\begin{split} F_L &= S_{1c}, \qquad P_1 = \frac{2S_3}{1 - F_L}, \\ P_2 &= \frac{2}{3} \frac{A_{FB}}{1 - F_L}, \qquad P_3 = \frac{-S_9}{(1 - F_L)}, \\ P'_4 &= \frac{S_4}{\sqrt{F_L(1 - F_L)}}, \qquad P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}, \\ P'_6 &= \frac{S_7}{\sqrt{F_L(1 - F_L)}}, \qquad P'_8 = \frac{S_8}{\sqrt{F_L(1 - F_L)}}, \end{split}$$

In total, 27 hadronic parameters !!!

Calculated in LCSR + QCDF

## Research procedures: $b \rightarrow s l l$ decays



## Statistics: $\chi^2$ fit & Frequentist analysis

$$\Box \chi^{2} \text{ fit}$$

$$\tilde{\chi}^{2}(\vec{\epsilon}, \vec{y}) = \chi^{2}_{\exp}(\vec{\epsilon}, \vec{y}) + \chi^{2}_{th}(\vec{y})$$

$$\chi^{2}_{\exp}(\vec{\epsilon}, \vec{y}) = [\vec{O}^{\text{th}}(\vec{\epsilon}, \vec{y}) - \vec{O}^{\exp}]^{T} \cdot (V^{\exp})^{-1} \cdot [\vec{O}^{\text{th}}(\vec{\epsilon}, \vec{y}) - \vec{O}^{\exp}],$$

$$\chi^{2}_{th}(\vec{y}) = (\vec{y} - \vec{y}_{0})^{T} \cdot (V^{th})^{-1} \cdot (\vec{y} - \vec{y}_{0}),$$

 $\vec{y}$  27 hadronic parameters (b $\rightarrow$ sll) 20 hadronic parameters (b $\rightarrow$  clv)  $\vec{\epsilon}$  Wilson coefficients

> The theory term is also parameterized in a Gaussian form

$$\chi_{\rm th}^2(\vec{y}) = \sum_i \left(\frac{y_i - \bar{y}_i}{\delta y_i}\right)^2,$$

> In order to obtain best-fit values in a particular scenario, we can construct a profile  $\chi^2$  depending only on certain Wilson coefficients

$$\chi^2(\vec{\epsilon}) = \min_{\vec{y}} \tilde{\chi}^2(\vec{\epsilon}, \vec{y})$$

### □ Frequentist analysis

> P-value: it is a statement how well the SM or BSM describes the data

 $\begin{aligned} \text{P-value}_{\text{SM}} &= 1 - \text{CDF}[\chi^2 \text{-distribution}[n_{\text{exp}}], \chi^2_{\text{min,SM}}] \\ \text{P-value}_{\text{NP}} &= 1 - \text{CDF}[\chi^2 \text{-distribution}[n_{\text{exp}} - n_{\epsilon}], \chi^2_{\text{min,NP}}] \end{aligned}$ 

> Pull<sub>SM</sub>: the significance of deviation from SM

$$\begin{split} &\Delta\chi^2_{\rm SM} = {\rm Quantile}[\chi^2 - {\rm distribution}[1], {\rm CDF}[\chi^2 - {\rm distribution}[n_\epsilon], \chi^2_{\rm min, SM} - \chi^2_{\rm min, NP}]] \\ &{\rm Pull}_{\rm SM} = \sqrt{\Delta\chi^2_{\rm SM}} \end{split}$$

The larger the p-value<sub>NP</sub>, the higher the significance of deviation from SM (the larger the  $Pull_{SM}$ ); but the smaller p-value<sub>SM</sub> tells us that the SM hypothesis under consideration may not adequately explain the data.



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## Latest experimental data

Observable	Observable Value		
	$(2.8^{+0.8}_{-0.7}) \times 10^{-9}$	ATLAS	ATLAS: JHEP04(2019)098
	$(2.9\pm0.7\pm0.2)\times10^{-9}$	CMS	CMS: JHEP04(2020)188
$BR(B_s \to \mu^+ \mu^-)$	$(3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$	LHCb update	Moriond 2021 seminar
	$(2.842 \pm 0.333) \times 10^{-9}$	our average	
	$(3.63 \pm 0.13) \times 10^{-9}$	SM prediction	
$R_{K}[1.1, 6]$	$0.846 \pm 0.044$	LHCb	Moriond 2021 seminar
$R_{K}[1, 6]$	$1.03\pm0.28$	Belle	Belle: JHEP03(2021)105
$R_{K^*}[0.045, 1.1]$	$0.660 \pm 0.113$	LHCb	1 HCb. 1HEP08(2017)055
$R_{K^*}[1.1, 6]$	$0.685 \pm 0.122$	LHCb	LINED. JILLI 00(2017)033
$R_{K^*}[0.045, 1.1]$	$0.52\pm0.365$	Belle	Pollo, DDI 126/2010/161901
$R_{K^*}[1.1, 6]$	$0.96 \pm 0.463$	Belle	Delle: PKL120(2019)101801

#### **Conservative** experimental uncertainties.

$$0.66^{+0.11}_{-0.07} \pm 0.03 
ightarrow 0.66 \pm \sqrt{0.11^2 + 0.03^2} = 0.66 \pm 0.113$$

## Clean Fit (2021 update)

 $\delta C_L^{\mu}$ 

-0.40



0.29

7.36 [6 dof]

$ (\delta C_9^{\mu}, \delta C_{10}^{\mu}) \ (-0.11, 0.59) \ 6.38 \ [5 \text{ dof}] \ 0.27 \ 4.62 \ \delta C_9^{\mu} \in [-0.41, \ 0.17] \ \delta C_{10}^{\mu} \in [0.38, \ 0.81] \ 0.762 $
Compared to the 2017 results, the significance of deviation from the SM has increased up to ~ $5\sigma$
Scenarios with pure axial currents, provide the best description of the data

[-0.48, -0.31]

[-0.66, -0.15]

4.89

30

## Global Fit (2021 update)



Coeff.	best fit	$\chi^2_{ m min}$	p-value	$\operatorname{Pull}_{\operatorname{SM}}$	$1\sigma$ range	$3\sigma$ range	ρ
$\delta C_9^{\mu}$	-0.85	106.32 [93 dof]	0.16	4.53	[-1.06, -0.64]	[-1.50, -0.27]	-
$\delta C^{\mu}_{10}$	0.54	107.82 [93 dof]	0.14	4.37	[0.41, 0.67]	[0.16, 0.94]	-
$\delta C_L^{\mu}$	-0.39	102.81 [93 dof]	0.23	4.91	$\left[-0.48,-0.31\right]$	$\left[-0.65, -0.15\right]$	_
$(\delta C_9^\mu, \delta C_{10}^\mu)$	(-0.56, 0.30)	102.36 [92 dof]	0.22	4.58	$\delta C_9^{\mu} \in [-0.79, -0.31]$	$\delta C_{10}^{\mu} \in [0.15, 0.49]$	0.317

Compared to the clean fit, δC<sub>9</sub> (δC<sub>10</sub>) is far away from (close to) the SM.
 Compared to the 2017 results, the value of δC<sub>9</sub> and δC<sub>10</sub> are better constrained.

## Robustness of fits with respect to hadronic uncertainties

#### **27** hadronic parameters in low q<sup>2</sup>: PRD93(1):014028,2016, JHEP, 05:043, 2013

QCDf(11)	$\mu, \xi_{\perp}(0), \xi_{\parallel}(0), f_{K^{\star}}, a1_{\perp}, a2_{\perp}(0), a1_{\parallel}(0), a2_{\parallel}(0), \omega_{0}, r_{\perp}, r_{\parallel}$
Power Corrections(8)	$V_{-}( a _{\max}), V_{-}( b _{\max}), V_{+}( a _{\max}), V_{+}( b _{\max}), T_{+}( b _{\max}), V_{0}( b _{\max}), T_{0}( a _{\max}), T_{0}( b _{\max})$
Charm contributions(8)	$h_{- c\bar{c}}( a _{\max}), h_{- c\bar{c}}( b _{\max}), \phi_{- c\bar{c}}, h_{+ c\bar{c}}( a _{\max}), h_{+ c\bar{c}}( b _{\max}), \phi_{+ c\bar{c}}, h_{0} _{c\bar{c}}, \phi_{0} _{c\bar{c}}$





□ Global fit result is sensitive to hadronic uncertainties. Therefore, hadronic uncertainties should be further studied in the future 32

- **\Box** Only operators  $O_9$ ,  $O_{10}$  can explain the experiment data
- □ We obtain conservative parameter space of new physics
- **\Box** Significance of the SM exclusion is ~ 5 $\sigma$
- □ Global fit result is sensitive to hadronic uncertainties which

should be future studied in the future



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□ Low energy effective Lagrangian

Jorge Martin Camalich et al, PRD94.094021

$$\mathcal{L}_{\text{eff}}^{\text{LE}} \supset -\frac{4G_F V_{cb}}{\sqrt{2}} [(1+\epsilon_L^{\tau})(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_R^{\tau}(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_R b) + \epsilon_{S_L}^{\tau}(\bar{\tau}P_L \nu_\tau)(\bar{c}P_L b) + \epsilon_{S_R}^{\tau}(\bar{\tau}P_L \nu_\tau)(\bar{c}P_R b) + \epsilon_T^{\tau}(\bar{\tau}\sigma_{\mu\nu}P_L \nu_\tau)(\bar{c}\sigma^{\mu\nu}P_L b)] + \text{H.c.}$$



- $\succ$  Wilson coefficients  $\epsilon$  stand for NP contributions.
- Right-handed vector cannot explain LUV 1505.05164. Consider

$$-\frac{4G_F V_{cb}}{\sqrt{2}} (\tilde{\epsilon}_R^\tau \bar{\tau} \gamma_\mu N_R) (\bar{c} \gamma^\mu P_R b) + 35$$

## Hadronic matrix elements in the $b \rightarrow c \tau v$ amplitudes

$$\begin{split} \langle D(k)|\bar{c}\gamma^{\mu}b|\bar{B}(p)\rangle &= (p+k)^{\mu}f_{+}(q^{2}) + (p-k)^{\mu}\frac{m_{B}^{2}-m_{D}^{2}}{q^{2}}(f_{0}(q^{2})-f_{+}(q^{2})), \\ \langle D(k)|\bar{c}b|\bar{B}(p)\rangle &= \frac{m_{B}^{2}-m_{D}^{2}}{m_{b}-m_{c}}f_{0}(q^{2}), \\ \langle D(k)|\bar{c}\sigma^{\mu\nu}b|\bar{B}(p)\rangle &= \frac{2if_{T}(q^{2})}{m_{B}+m_{D}}(k^{\mu}p^{\nu}-p^{\mu}k^{\nu}), \\ \langle D(k)|\bar{c}\sigma^{\mu\nu}\gamma_{5}b|\bar{B}(p)\rangle &= \frac{2f_{T}(q^{2})}{m_{B}+m_{D}}\epsilon^{\mu\nu\alpha\beta}k_{\alpha}p_{\beta}, \\ \langle V(k,\epsilon)|\bar{c}\gamma^{\mu}b|P(p)\rangle &= \frac{2iV(q^{2})}{m_{P}+m_{V}}\epsilon^{\mu\nu\alpha\beta}\epsilon^{*}_{\nu}k_{\alpha}p_{\beta}, \\ \langle V(k,\epsilon)|\bar{c}\gamma^{\mu}\gamma_{5}b|P(p)\rangle &= -\frac{2m_{V}}{m_{b}+m_{c}}A_{0}(q^{2})\epsilon^{*}\cdot q, \\ \langle V(k,\epsilon)|\bar{c}\gamma^{\mu}\gamma_{5}b|P(p)\rangle &= 2m_{V}A_{0}(q^{2})\frac{\epsilon^{*}\cdot q}{q^{2}}q^{\mu} + (m_{P}+m_{V})A_{1}(q^{2})\left(\epsilon^{*\mu}-\frac{\epsilon^{*}\cdot q}{q^{2}}q^{\mu}\right) \\ &-A_{2}(q^{2})\frac{\epsilon^{*}\cdot q}{m_{P}+m_{V}}\left((p+k)^{\mu}-\frac{m_{P}^{2}-m_{V}^{2}}{q^{2}}q^{\mu}\right) \\ \langle V(k,\epsilon)|\bar{c}\sigma^{\mu\nu}b|P(p)\rangle &= \frac{\epsilon^{*}\cdot q}{(m_{P}+m_{V})^{2}}T_{0}(q^{2})\epsilon^{\mu\nu\alpha\beta}p_{\alpha}k_{\beta} \\ &+T_{1}(q^{2})\epsilon^{\mu\nu\alpha\beta}p_{\alpha}\epsilon^{*}_{\beta} + T_{2}(q^{2})\epsilon^{\mu\nu\alpha\beta}k_{\alpha}\epsilon^{*}_{\beta}, \\ \langle V(k,\epsilon)|\bar{c}\sigma^{\mu\nu}\gamma_{5}b|P(p)\rangle &= \frac{i\epsilon^{*}\cdot q}{(m_{P}+m_{V})^{2}}T_{0}(q^{2})(p^{\mu}k^{\nu}-k^{\mu}p^{\nu}) \\ &+iT_{1}(q^{2})(p^{\mu}\epsilon^{*\nu}-\epsilon^{*\mu}p^{\nu}) + iT_{2}(q^{2})(k^{\mu}\epsilon^{*\nu}-\epsilon^{*\mu}k^{\nu}), \end{split}$$



**Decay constant:** 

→  $B_c \rightarrow \tau \nu$ : LQCD HPQCD: PRD91.114509

#### **Given Form factors :**

- ►  $B \rightarrow D^{(*)} \tau \nu$ : HQET(LO) & fitting to data & LQCD Jorge Martin Camalich et al, PRD94.094021
- →  $B_c \rightarrow J/\psi \tau \nu$ : covariant light-front quark model (LFQM) Cai-Dian Lv et al, PRD79.054012

				the most r	eliable
Observables		Data (a	verages)		SM
	HFLA	V 2018	HFLA	2019	
$R_D$	0.407(39)(24)		0.340(27)(13)		0.312(19)
		corr = -0.20		corr = -0.38	
$R_{D^*}$	0.306(13)(7)		0.295(11)(8)		0.253(4)
$R_{J/\psi}$		0.71(1	7)(18)		0.248(3)
$P^{D^*}_{ au}$		-0.505(23)			
$F_L^{D^*}$		0.455(9)			

## **□** Further observables $\tau$ polarization asymmetry $P_{\tau}^{D^*}$ and the longitudinal polarization of D ( $F_L^{D^*}$ ) in the $B \rightarrow D^* \tau \nu$ decay:

$$P_{\tau}^{D^*} = \frac{\Gamma(\lambda_{\tau} = \frac{1}{2}) - \Gamma(\lambda_{\tau} = -\frac{1}{2})}{\Gamma(\lambda_{\tau} = \frac{1}{2}) + \Gamma(\lambda_{\tau} = -\frac{1}{2})}, \qquad R_{J/\psi} = \frac{\Gamma(B_c \to J/\psi\tau\bar{\nu})}{\Gamma(B_c \to J/\psi\mu\bar{\nu})}$$
$$F_L^{D^*} = \frac{\Gamma(\lambda_{D^*} = 0)}{\Gamma(\lambda_{D^*} = 1) + \Gamma(\lambda_{D^*} = 0) + \Gamma(\lambda_{D^*} = -1)}, \qquad R_{J/\psi} = \frac{\Gamma(B_c \to J/\psi\tau\bar{\nu})}{\Gamma(B_c \to J/\psi\mu\bar{\nu})}$$

Tension with SM~2 $\sigma$ , but the significance of  $R_{J/\psi}$  is less than 4 $\sigma$ .

## Fits to $R_D$ and $R_{D^*}$ only



- > New Belle measurement with semileptonic tag
- > 2018HFLAV
- The combination of the above two

$$\succ \quad \text{Vector: } \epsilon_L^\tau \text{ or } \tilde{\epsilon}_R^\tau$$

Scalar-Tensor 
$$\epsilon_{SL}^{\tau} = -4\epsilon_{T}^{\tau}$$

 $\succ$  Tensor  $\epsilon_T^{\tau}$ 

- 2018 HFLAV, only vector and scalar-tensor works
- □ After Belle, tensor also works

## Fits to $R_D$ and $R_{D^*}$ only



- **D** Dotted lines show that the significance of deviation from SM is more than  $3\sigma$ .
- **The (left)vector and tensor operators give better fits to the data (than the other two).**
- **The**  $\chi^2$  difference shows that the 2018 HFLAV data are in conflict with the 2019 HFLAV data.

## Fits to $R_D$ and $R_{D^*}$ only : six 2D plots



## Fits to $R_D$ and $R_{D^*}$ only

 $\chi^2_{SM} = 20.75$  p-value in SM : 1.38×10<sup>-2</sup>

	Best fit	$\chi^2_{\rm min}$	p-value	Pull <sub>SM</sub>	$1\sigma$ range	
$\epsilon_L^{ au}$	0.07	9.00	0.34	3.43	(0.05, 0.09)	
$\epsilon_T^{ au}$	-0.03	9.85	0.28	3.30	(-0.04, -0.02)	
$\epsilon_{S_I}^{ au}$	0.09	19.14	$1.41 \times 10^{-2}$	1.27	(0.02, 0.15)	
$\epsilon^{ au}_{S_{H}}$	0.13	15.84	$4.47\times10^{-2}$	2.22	(0.07, 0.20)	
$\tilde{\epsilon}_R^{ au}$	0.38	9.00	0.34	3.43	(0.32, 0.44)	
$\epsilon^{\tau}_{S_L} = -$	$-4\epsilon_T^{\tau}$ 0.09	12.25	0.14	2.92	(0.06, 0.12)	
$(\epsilon_{S_L}^{\tau},$	$\epsilon_T^{\tau}$ ) (0.07, -0.03)	8.7	0.27	3.03	$\epsilon^{\tau}_{S_L} \in (0.00, 0.14)$ $\epsilon^{\tau}_T \in (-0.04, -0.02)$	
$(\epsilon_{S_L}^{ au}, \epsilon_{S_L})$	(-0.47, 0.53)	8.7	0.27	3.03	$\epsilon_{S_L}^{\tau} \in (-0.66, -0.30)  \epsilon_{S_R}^{\tau} \in (0.37, 0.69)$	
$(\epsilon_{S_R}^{\tau},$	$\epsilon_T^{\tau}$ ) (0.07, -0.03)	8.7	0.27	3.03	$\epsilon^{\tau}_{S_R} \in (0.00, 0.14)  \epsilon^{\tau}_T \in (-0.04, -0.02)$	
$(\epsilon_L^{ au},\epsilon_L^{ au})$	(0.05, -0.01)	8.7	0.27	3.03	$\epsilon_L^\tau \in (0.00, 0.09)  \epsilon_T^\tau \in (-0.03, 0.01)$	
$(\epsilon_L^{ au},\epsilon)$	${}^{\tau}_{S_L}$ ) (0.08, -0.04)	8.7	0.27	3.03	$\epsilon_L^{\tau} \in (0.05, 0.10)  \epsilon_{S_L}^{\tau} \in (-0.13, 0.04)$	
$(\epsilon_L^{ au},\epsilon)$	(0.08, -0.05)	8.7	0.27	3.03	$\epsilon_L^{\tau} \in (0.05, 0.11)$ $\epsilon_{S_R}^{\tau} \in (-0.15, 0.04)$	

- □ Vectors are the best. Scalars are ruled out
- $\hfill\square$  The significance of deviation from SM is more than  $3\sigma$



□ For example, assuming NP couplings are of O(1) order:

Scalar LQ

```
> Vector LQ
```

```
m_{\mathbf{S_1}} pprox m_{\mathbf{S_3}} pprox m_{\mathbf{R_2}} pprox \mathbf{2.3 ~TeV}
```

 $m_{U_1}\approx m_{U_3}\approx 3.3~TeV$ 

### Fits to all the 2019 HFLAV data



## Fits to all the 2019 HFLAV data

 $\chi^2_{min,SM} = 26.53$  p-value in SM : 9.02×10<sup>-3</sup>

		Best fit	$\chi^2_{\rm min}$	p-value	Pull <sub>SM</sub>	$1\sigma$ range	
$\epsilon_L^{\tau}$		0.07	14.56	0.20	3.46	(0.05, 0.09)	
$\epsilon_T^{ au}$		-0.03	15.70	0.15	3.29	(-0.04, -0.02)	
$\epsilon_{S_{II}}^{\tau}$	ı.	0.08	25.23	$8.44 \times 10^{-3}$	1.14	(0.01, 0.14)	
$\epsilon_{S_{I}}^{\tau}$	2	0.14	21.24	$3.10  imes 10^{-2}$	2.30	(0.08, 0.20)	
$(\epsilon_{S_L}^{\tau},$	$\epsilon_T^{\tau}$ ) (	(0.07, -0.03)	14.75	0.14	3.00	$\epsilon_{S_L}^{\tau} \in (0.00, 0.13)  \epsilon_T^{\tau} \in (-0.04, -0.02)$	
$(\epsilon_{S_L}^{\tau},\epsilon)$	$\epsilon_{S_R}^{\tau}$ ) (	(-0.51, 0.56)	12.14	0.28	3.37	$\epsilon_{S_L}^{\tau} \in (-0.69, -0.34)$ $\epsilon_{S_R}^{\tau} \in (0.41, 0.73)$	
$(\epsilon_{S_R}^{\tau},$	$\epsilon_T^{\tau}$ ) (	(0.08, -0.03)	14.38	0.16	3.05	$\epsilon_{S_R}^{\tau} \in (0.01, 0.14)  \epsilon_T^{\tau} \in (-0.04, -0.02)$	
$(\epsilon_L^{ au},\epsilon_L^{ au})$	$\epsilon_T^{\tau}$ ) (	(0.05, -0.01)	14.32	0.16	3.06	$\epsilon_L^{\tau} \in (0.01, 0.10)$ $\epsilon_T^{\tau} \in (-0.03, 0.01)$	
$(\epsilon_L^{\tau},\epsilon)$	$\left( \frac{\tau}{S_L} \right)$ (	(0.08, -0.06)	14.09	0.17	3.09	$\epsilon_L^{\tau} \in (0.06, 0.10)$ $\epsilon_{S_L}^{\tau} \in (-0.14, 0.03)$	
$(\epsilon_L^{\tau},\epsilon)$	$\left(\frac{\tau}{S_R}\right)$	(0.08, -0.05)	14.33	0.16	3.06	$\epsilon_L^{\tau} \in (0.05, 0.11)$ $\epsilon_{S_R}^{\tau} \in (-0.14, 0.05)$	

#### □ Scalar disfavored

 $\Box$  The significance of deviation from SM is more than 3 $\sigma$ .

## Possibility of discriminating different NP structures: only fitting to R<sub>D</sub> and R<sub>D\*</sub>



A measurement of the tau polarization in the decay mode  $B \rightarrow D \tau \nu$  would effectively discriminate different NP scenarios.

## Possibility of discriminating different NP structure

Observables	bservables SM	$\epsilon_T^{\tau} = -0.03$	$(\epsilon^{\tau}_{S_L}, \epsilon^{\tau}_T)$	$(\epsilon_L^{\tau}, \epsilon_{S_R}^{\tau})$	$(\epsilon_L^{\tau}, \epsilon_T^{\tau}, \epsilon_{S_L}^{\tau}, \epsilon_{S_R}^{\tau})$
Observables			= (0.07, -0.03)	= (0.08, -0.05)	= (0.16, 0.05, -0.33, 0.14)
$R_D$	$0.312^{+0.019}_{-0.018}$	$0.303^{+0.019}_{-0.018}$	$0.340^{+0.023}_{-0.021}$	$0.339^{+0.020}_{-0.018}$	0.343 <sup>+0.017</sup> 0.016
$P^D_{ au}$	$0.338^{+0.033}_{-0.034}$	$0.358^{+0.033}_{-0.034}$	$0.427^{+0.032}_{-0.032}$	$0.288^{+0.034}_{-0.034}$	$0.117^{+0.033}_{-0.033}$
$A^D_{FB}$	$-0.358^{+0.003}_{-0.003}$	$-0.344^{+0.004}_{-0.003}$	$-0.334^{+0.005}_{-0.004}$	$-0.363^{+0.002}_{-0.002}$	$-0.383^{+0.002}_{-0.001}$
$R_{D^*}$	$0.253^{+0.004}_{-0.004}$	$0.293\substack{+0.004\\-0.004}$	$0.291^{+0.004}_{-0.003}$	$0.293^{+0.004}_{-0.004}$	$0.297^{+0.009}_{-0.008}$
$P_{ au}^{D^{\star}}$	$-0.505^{+0.024}_{-0.022}$	$-0.477^{+0.020}_{-0.019}$	$-0.487^{+0.019}_{-0.017}$	$-0.513^{+0.023}_{-0.021}$	$-0.430^{+0.042}_{-0.041}$
$A_{FB}^{D^*}$	$0.068^{+0.013}_{-0.013}$	$0.030\substack{+0.012\\-0.012}$	$0.038^{+0.012}_{-0.012}$	$0.073^{+0.013}_{-0.013}$	$0.083^{+0.017}_{-0.016}$
$F_L^{D^{\star}}$	$0.455^{+0.009}_{-0.008}$	$0.444^{+0.008}_{-0.007}$	$0.440^{+0.007}_{-0.007}$	$0.452^{+0.008}_{-0.008}$	$0.497^{+0.015}_{-0.014}$
$R_{J/\psi}$	$0.248^{+0.003}_{-0.003}$	$0.291^{+0.004}_{-0.004}$	$0.289^{+0.004}_{-0.004}$	$0.288^{+0.004}_{-0.004}$	$0.284^{+0.003}_{-0.003}$
$P_{ au}^{J/\psi}$	$-0.512^{+0.011}_{-0.010}$	$-0.481\substack{+0.009\\-0.008}$	$-0.490^{+0.008}_{-0.008}$	$-0.519^{+0.010}_{-0.010}$	$-0.453^{+0.020}_{-0.019}$
$A_{FB}^{J/\psi}$	$0.042\substack{+0.006\\-0.006}$	$0.007\substack{+0.006\\-0.006}$	$0.013^{+0.006}_{-0.006}$	$0.046^{+0.006}_{-0.006}$	$0.061^{+0.007}_{-0.007}$
$F_L^{J/\psi}$	$0.446^{+0.003}_{-0.003}$	$0.434^{+0.003}_{-0.003}$	$0.430^{+0.002}_{-0.002}$	$0.443^{+0.003}_{-0.003}$	$0.490^{+0.005}_{-0.005}$

Indeed,  $P_{\tau}^{D}$  is an excellent observable which can be measured in Belle II and upgraded LHCb.

No corresponding NP

- **\Box** Significance of the SM exclusion is more than  $3\sigma$ .
- □ BR( $B_c \rightarrow \tau \nu$ ), the LHC monotau and  $F_L^{D^*}$  can exclude large regions of the parameter space.
- □ We tested some NP models in which LQs can explain the data.
- □ We also found that the **T** polarization  $P_{\tau}^{D}$  in the B→D  $\tau \nu$  decay is sensitive to the various new-physics scenarios which are favored by the current data.



## Background

- □ Theoretical framework
- Results and discussions
  - > Flavor-changing-neutral-current(FCNC)  $b \rightarrow s l l$  decays
  - > Charged-current(CC)  $b \rightarrow c \tau \nu$  decays
- □ Summary and outlook

## **Summary and Outlook**

- **\Box** Significance of the SM exclusion for  $b \rightarrow s l l$  transition is ~ 5 $\sigma$
- □ Significance of the SM exclusion for  $b \rightarrow c \tau v$  transition is more than 3σ
- We also test some NP models, only some LQs can explain the current data
- □ We also found that the **T** polarization  $P_{\tau}^{D}$  in the B→D  $\tau \nu$  decay is sensitive to the various new-physics scenarios which are favored by the current data

In the next few years, with the collection of more data at the B factories and improvement of experimental precision:

- □ We will continually update our analysis.
- In addition, new theoretical works on the theoretical side will be needed to better assess uncertainties.
  - > Form factors and charm contributions for  $b \rightarrow s l l$  transition
  - **>** Form factors for  $b \rightarrow c \tau \nu$  transition
- Meantime, it is also important to continue to find or construct new observables which are very sensitive to new physics.





## **Thanks for your attention!**



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# **Backup slides**

### **Right-handed vector operator cannot explain LUV**

#### SMEFT

#### LEEFT



NP particles do not directly couple to two leptons in the two-Higgs model. Therefore, the right-handed vector operator cannot contribute to and explain lepton universality violation.

## 4D global fit for $b \rightarrow c \tau \nu$ decays

